
	<p>Pimpri Chinchwad Education Trust's  <b>S.B. PATIL COLLEGE OF SCIENCE &amp; COMMERCE, RAVET</b>          Sr. no. 110, Gate No 1, Ravet, Pune- 412101  <a href="http://www.sbpatilcollege.com">www.sbpatilcollege.com</a>, <a href="mailto:email-sbpc.science@gmail.com">email-sbpc.science@gmail.com</a>          UDISE NO: 27252001412      College Index No: J.11.16.066</p>	
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**Annual Exam (2019-2020)**

**Sub :- Mathematics(Science)**

**Marks-80**

**Std- 11<sup>th</sup> Date :- 18/3/20**

**Time-3hr**

**General Instructions:-** The question paper is divided in to four sections.

- 1. Section A :** Q.No. 1 contains eight multiple choice type of questions carrying **Two** marks each.  
Q.No.2 contains four very short answer type of questions carrying **one** mark each.
- 2. Section B :** Q.No.3 to Q.No.14 contains Twelve short answer type of questions carrying **Two** marks each.
- 3. Section C :** Q.No.15 to Q.No.26 contains Twelve short answer type of questions carrying **Three** marks each.
- 4. Section D :** Q.No.27 to Q.No.34 contains Eight long answer type of questions carrying **Four** marks each.
- 5.** Use of log table is allowed. Use of calculator is not allowed.

**Section - A**

**Q.1 Select and write the correct answer.**

**[16]**

1.  $(\frac{11\pi}{15})^c$  is equal to ,-----  
 a)  $123^0$       b)  $132^0$       c)  $112^0$       d)  $213^0$
2.  $\sqrt{-18}i =$  -----  
 a)  $-3\sqrt{2}$       b)  $3\sqrt{2}$       c)  $3\sqrt{2}i$       d)  $-3\sqrt{2}i$
3. The sum of three terms of a G.P is  $\frac{21}{4}$  and their product is 1 , then the common ratio is  
 a) 3      b) 2      c) 4      d) -1
4. If  $\log_{10}(\log_{10}(\log_{10} x)) = 0$  then x = -----  
 a) 1000      b)  $10^{10}$       c) 10      d) 0

5. In how many ways 4 boys and 3 girls can be seated in a row such that they are alternate
- a) 12      b) 288      c) 144      d) 256
6. If  $A = \begin{bmatrix} a & 2 \\ 2 & a \end{bmatrix}$  and  $|A^3| = 125$ , then  $a = ?$
- a)  $\pm 3$       b)  $\pm 2$       c)  $\pm 5$       d) 0
7. The equation of the line through (2,2) which makes equal intercepts on the axes is ,
- a)  $x + y = 1$       b)  $x + y = 2$       c)  $x + y = 4$       d)  $x + y = 5$
8. The length of latus rectum of the parabola  $x^2 - 4x - 8y + 12 = 0$  is
- a) 4      b) 6      c) 8      d) 10.

**Q.2 Answer the following**

**[4]**

- Find the equation of the ellipse whose centre is O (0,0) focus at (2,0) and eccentricity is  $1/2$
- Find the value of  $\tan 75^\circ$ .
- Find the number of 4 digit even numbers formed with the digits 1,2,3, & 4
- If  $f(x) = x^2$  and  $g(x) = \frac{5x-6}{7}$  then find the value of  $g(f(x))$  at  $x=0$

**Section –B**

**Attempt any Eight of the following .**

**[16]**

- Q.3 Find m and n if ,  $(2m-n) + (m+2n)i = 8+5i$
- Q. 4 Find the sum of n terms,  $2 + 22 + 222 + 2222 + \dots$
- Q.5 Find n if ,  ${}_{23}C_{3n} = {}_{23}C_{2n+3}$ .
- Q.6 If  $f(x) = 2x^2 + 3$  ,  $g(x) = 5x-2$  then find ,
- a) fog      b) gof
- Q.7 Evaluate ,  $\lim_{x \rightarrow 0} \frac{\sin x \cdot \tan x}{x \log(1+2x)}$
- Q.8 Find the distance of the point(2,2) from the line  $3x-4y+10=0$
- Q.9 If o be the origin and A and B be the point of intersection of the line  $3x-5y = 15$  withn the axes then find the area of the triangle AOB.
- Q.10 If  $A+B+C = \pi$  then Prove that  $\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$
- Q.11 Find x and y if ,  $\begin{bmatrix} 2x+y & -1 & 1 \\ 3 & 4y & 4 \end{bmatrix} + \begin{bmatrix} -1 & 6 & 4 \\ 3 & 0 & 3 \end{bmatrix} = \begin{bmatrix} 3 & 5 & 5 \\ 6 & 18 & 7 \end{bmatrix}$
- Q. 12 Write the equation of line parallel to  $x+y=2$  and at a distance of 4 unit from it.
- Q.13 Find the equation of ellipse in the standard form ,if length of major axis 10 and distance between foci is 8.
- Q.14 Find the radius and the centre of the circle  $x^2 + y^2 - 12x + 18y - 11 = 0$  .

## Section C

Attempt any Eight of the following .

[24]

Q.15 Find the common ratio of a G.P if sum to infinity is 12 and the first term is 2.

Q.16 Find the distance between the lines  $3x - 4y - 7 = 0$  and  $6x - 8y + 18 = 0$ .

Q.17 If  $\frac{x^2}{25} - \frac{y^2}{16} = 1$  be the equation of an ellipse then find the length of transverse axis , length of conjugate axis, the eccentricity of hyperbola and the length of its latusrectum.

Q.18 Find the area of the triangle formed by a chord that subtend an angle of  $45^\circ$  at the centre of the circle of radius 16 units.

Q.19 Find n , if  $\frac{(17-n)!}{(14-n)!} = 5!$

Q.20 Find the value of ,  $(\sqrt{3} + i)^4 + (\sqrt{3} - i)^4$

Q.21 If A and B are subsets of universal set X and  $n(X) = 50$  ,  $n(A) = 35$  ,  $n(B) = 20$  ,  $n(A' \cap B') = 5$  find ,  
1)  $n(A \cup B)$  2)  $n(A \cap B)$  3)  $n(A' \cap B)$

Q.22 If  $f(x) = x^2 + 3$   $x \leq 2$   
 $= 5x + 7$   $x > 2$  then find , 1)  $f(3)$  2)  $f(2)$  3)  $f(0)$

Q.23 Evaluate,  $\lim_{x \rightarrow 0} \frac{x \tan x}{1 - \cos x}$

Q.24 Test the continuity of the following function at the points indicated against them,

$$f(x) = \frac{x^3 - 8}{\sqrt{x+2} - \sqrt{3x-2}} \text{ for } x \neq 2$$
$$= -24 \text{ for } x = 2 \text{ at } x = 2$$

Q.25 Differentiate with respect to x ,  $y = e^x \cdot \log x$

Q.26 If  $A = \begin{bmatrix} 1 & -1 & 2 \\ -2 & 1 & 0 \end{bmatrix}$   $B = \begin{bmatrix} 2 & -4 \\ 3 & -2 \\ 0 & 1 \end{bmatrix}$  prove that ,  $(A + B^T)^T = A^T + B$

## Section D

Attempt any Five of the following .

[20]

Q.27 5 students are selected at random from 11 students. How many ways can these be done if-

- (a). Two specific students are selected?
- (b). Two specific students are not selected?

Q.28 If  $\log\left(\frac{x+y}{3}\right) = \frac{1}{2} \log x + \frac{1}{2} \log y$  , then show that  $\frac{x}{y} + \frac{y}{x} = 7$

Q.29 In a class of 200 students who appeared certain examinations ,35 students failed in CET , 40 in NEET and 40 in JEE ,20 failed in CET and NEET , 17 in NEET and JEE ,15 in CET and JEE and 5 failed in all three examination . find how many students ,

- 1) Did not fail in any exam
- 2) Failed in NEET or JEE entrance.

Q.30 Evaluate,  $\lim_{x \rightarrow 0} \frac{6^x + 5^x + 4^x - 3^{x+1}}{\sin x}$

Q.31 If  $f(x) = \frac{24^x - 8^x - 3^{x+1}}{12^x - 4^x - 3^{x+1}}$ , for  $x \neq 0$   
= k for  $x=0$  is continuous at  $x=0$ , then find k.

Q.32 Find the derivatives of  $\cos x$  by using first principle.

Q.33 If  $A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$  show that  $A^2 - 5A - 14A = 0$

Q.34 If the coefficient of  $x^2$  in  $(1 + 2x)^m$  is 112 then find the coefficient of  $x^6$ .

